

Code: 23BS1101

I B.Tech - I Semester – Supplementary Examinations – MAY 2025**LINEAR ALGEBRA & CALCULUS**
(Common for ALL BRANCHES)

Duration: 3 hours

Max. Marks: 70

Note: 1. This question paper contains two Parts A and B.

2. Part-A contains 10 short answer questions. Each Question carries 2 Marks.

3. Part-B contains 5 essay questions with an internal choice from each unit. Each Question carries 10 marks.

4. All parts of Question paper must be answered in one place.

PART – A

1.a)	Define Normal form.
1.b)	Write Consistency conditions for Homogeneous linear system of equations.
1.c)	If $A = \begin{bmatrix} -1 & 2 & 3 \\ 0 & 3 & 5 \\ 0 & 0 & -2 \end{bmatrix}$, then find the eigen values of A^{-1}
1.d)	Verify Cayley-Hamilton theorem for $\begin{bmatrix} 5 & 3 \\ 3 & 2 \end{bmatrix}$.
1.e)	State Cauchy Mean Value Theorem.
1.f)	Write the Taylor's Series of $\cos x$ about $\frac{\pi}{4}$.
1.g)	Define Jacobian of 3 variables.
1.h)	If $x = r \cos \theta$, $y = r \sin \theta$, show that $\frac{\partial(x, y)}{\partial(r, \theta)} = r$.
1.i)	Evaluate $\int_1^2 \int_1^3 xy^2 dx dy$
1.j)	Write the formula to find volume in Cartesian form.

PART – B

					Max. Marks
UNIT-I					
2	a)	Find rank by reducing $\begin{bmatrix} -2 & -1 & -3 & -1 \\ 1 & 2 & 3 & -1 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & -1 \end{bmatrix}$ into Echelon form.			5 M
	b)	Solve $x+y+z = 6$; $x-y+2z = 5$; $2x-2y+3z = 7$.			5 M
OR					
3	a)	Find rank of $A=\begin{bmatrix} 0 & 1 & 2 & -2 \\ 4 & 0 & 2 & 6 \\ 2 & 1 & 3 & 1 \end{bmatrix}$ by reducing into Echelon form.			5 M
	b)	Solve $10x_1 + x_2 + x_3 = 12$; $2x_1 + 10x_2 + x_3 = 13$; $2x_1 + 2x_2 + 10x_3 = 14$ by Gauss Seidel method.			5 M
UNIT-II					
4	a)	Find Eigen values and Eigen vectors of $A=\begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$			5 M
	b)	Verify Cayley-Hamilton theorem for $A=\begin{bmatrix} 2 & 5 & 5 \\ 0 & 3 & 0 \\ 5 & 5 & 8 \end{bmatrix}$ and hence find A^{-1} and A^4 .			5 M
OR					

5		Reduce the quadratic form $6x^2 + 3y^2 + 3z^2 - 4xy + 4xz - 2yz$ in to canonical form by orthogonal transformation method. Find Index, Rank, Signature, Nature of the quadratic form.	10 M
UNIT-III			
6	a)	Verify Rolle's theorem for the function $f(x) = x^3 - 4x + 8$ in the interval $[-2, 2]$.	5 M
	b)	Expand $\sin x$ by Maclaurin's series up to the term containing x^5 .	5 M
OR			
7	a)	Find $\sqrt[5]{245}$ using Lagrange's mean value theorem.	5 M
	b)	Verify Cauchy's mean value theorem for the function $f(x) = \sqrt{x}, g(x) = \frac{1}{\sqrt{x}}$ in the interval $[a, b]$.	5 M
UNIT-IV			
8	a)	If $x + y + z = u, y + z = uv, z = uvw$ then find $J\left(\frac{x, y, z}{u, v, w}\right)$.	5 M
	b)	Expand $\cos x \cos y$ in powers of x and y .	5 M
OR			
9	a)	If $u = f[(y - z), (z - x), (x - y)]$ then show that $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = 0$	5 M
	b)	In a plane triangle ABC, find the maximum value of $\cos A \cos B \cos C$.	5 M

UNIT-V

10	a)	Evaluate $\iint_R \frac{x^2 y^2}{(x^2 + y^2)} dx dy$ where R is the annular region between two circles $x^2 + y^2 = a^2$ and $x^2 + y^2 = b^2$ ($b > a$).	5 M
	b)	Evaluate $\int_0^1 \int_0^x e^{y/x} dy dx$	5 M
OR			
11	a)	Evaluate $\iint_R xy(x+y) dx dy$, where R is the region bounded by $y = x^2$ and $y = x$	5 M
	b)	Evaluate $\int_0^\infty \int_0^\infty e^{-(x^2+y^2)} dx dy$	5 M